| From: | Peralta, Rene (Fed) |
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| To: | Calik, Cagdas (Int1Assoc) |
| CC: | Sonmez Turan, Meltem (Fed); ;eralta, Rene C. (Fed) |
| Subject: | Re: MC of the Counting function (8,4) is 6. |
| Date: | Thursday, September 15, 2016 6:35:46 PM |
| Attachments: | MultComp3.pdf |

Great. I have a PQC meeting tomorrow, but maybe I will skip it. Let us play it by ear.

I am attaching what I think is the proof we needed (I think what you wanted is that the multiplicative complexity of
$u v f$
(where $u, v$ are variables and $f$ is a function of variables other than $u, v$ )
is $1+$ mult_comp( v f)

That is a corollary of the claim in the attached.

Regards, Rene.
$* * * * * * * * * * * * * * * * * * * * * * * *$
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From: Calik, Cagdas (Int|Assoc)
Sent: Thursday, September 15, 2016 4:48 PM
To: Peralta, Rene (Fed)
Cc: Sonmez Turan, Meltem (Assoc)
Subject: MC of the Counting function $(8,4)$ is 6 .
Hi Rene,
By using the same approach (reducing the number of variables after affine transformations) we were
able to find a 6 multiplication implementation of the counting function $E(8,4)$. In your "Tight Bounds..." paper with Joan, the MC of this function was left as an open question, it could be either 6 or 7 .
We hope to give you the details of the implementation tomorrow morning. Cagdas \& Meltem

